A Novel Algorithm for Rotor Speed Estimation of DFIGs Using Machine Active Power based on MRAS Observer

R. Ajabi-Farshbaf *, M. R. Azizian, V. Yousefizad
Faculty of Electrical Engineering, Sahand University of Technology (SUT), Tabriz, Iran.

Abstract—This paper presents a new algorithm based on Model Reference Adaptive System (MRAS) and its stability analysis for sensorless control of Doubly-Fed Induction Generators (DFIGs). The reference and adjustable models of the suggested observer are based on the active power of the machine. A hysteresis block is used in the structure of the adaptation mechanism, and the stability analysis is performed based on sliding mode conditions. Simulation and practical results show appropriate operation and speed tracking of the observer with regard to obtained stability conditions.

Keyword: Active power; Doubly fed induction generator; MRAS-based observer; Stability analysis.

NOMENCLATURE

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$est$ Estimation value

1. INTRODUCTION

Generally, machine speed data is needed to implement most of control strategies, especially vector control [1]. Tachogenerators, resolvers, incremental and light encoders are common-used speed sensors, which may cause some problems. These sensors reduce system reliability and require accurate installation and calibration, maintenance, extra cabling, and immunizing against electric noises. Furthermore, in some applications, it is difficult to construct speed feedback. Installation and maintenance of speed sensors in wind turbines and generators with high height is a time-consuming and costly act. Therefore, sensor elimination leads to significant facilities. When speed sensors fail, the system controller receives incorrect feedback signals, which disrupts its operation [2].

Many speed estimation strategies are developed and explained in previously reported works. Some of Basic methods are explained in [3] for induction machines. Speed estimation algorithms for Doubly-Fed Induction Machines (DFIMs) and DFIGs are generally developed forms of basic algorithms. Speed estimation algorithms for Doubly-Fed Induction Machines (DFIMs) and DFIGs are generally developed forms of basic algorithms. Especially in DFIG, rotor-side parameters are measureable and therefore they can be used in the estimation algorithms. Some of basic methods are classified as follows:

- MRAS based algorithms; in [4] basic structure of MRAS is changed to be applied in DFIG where a new adaptation
mechanism and new state variables are selected. Four MRAS-based observers are evaluated in [5] for DFIGs. State variables of the proposed observers are different. In [6], another MRAS observer is introduced for DFIMs where its main specification is direct estimation of torque and rotor flux components. The suggested MRAS algorithm in [7], applies a constant gain in the adjustable model of the MRAS which solves drift problems of integrators. In [8] a MRAS algorithm is developed which is based on neural networks. In the MRAS observer proposed in [9], machine reactive power is used as a new adaptation mechanism. In [10], air-gap electromagnetic force (EMF) is defined as the working variable and MRAS control strategy is considered to calculate the rotor position.

Adaptive observers; in [11], an adaptive observer, which is an extension of the basic Luenberger algorithm, is designed for sensorless control of DFIGs. A reduced-order adaptive observer is explained in [12] for stator flux and speed estimation. Structure of the conventional Kalman filter is changed in [13] to be used for sensorless control of DFIM. Rotor side measurements is also applied in the proposed algorithm. In [14], another reduced-order adaptive observer is presented for DFIG. It is also based on Luenberger observer and contains different state variables.

Other methods: A straightforward algorithm is designed in [15] for rotor position estimation, in which flux calculations and integrators not included. Speed estimation from machine slip is explained in [16]. In [17], a sensorless control strategy is developed which is based on the Phase-Locked Loop (PLL) system. According to the authors’ discussion, it is independent of machine parameters. The presented algorithm in [18] is relatively simple and contains no flux calculations. Undesired effects of integrators is reduced in [18] which is its main advantage.

According to the numerous works reported in the literature, MRAS based observers have proved to provide more acceptable operation, especially with the state variable, which is independent from machine fluxes. Based on reported works evaluation, an adaptive observer consists of system model, adaptation mechanism, a term for model correction and stability analysis. In all reported works one or more of these parts have designed with a new procedure. Therefore, in this paper, a new MRAS based speed estimation algorithm is introduced. Compared with previously reported works in this paper a hysteresis block is used in the structure of the adaptation mechanism, and the stability analysis is performed based on sliding mode conditions. Purposed method stability and parameter sensitivity is analysed with extensive formulation. Active power of the machine is considered as state variable of the proposed method and a new adaptation mechanism is extracted. Therefore, the proposed method in this paper is a completely new algorithm and its equations is exclusive to suggested model because:

1- It is based on DFIG active power.
2- The suggested adaptation mechanism is based on a hysteresis block.
3- Stability study is performed based on operation of the hysteresis controller and sliding mode conditions.

Since the proposed method is based on hysteresis analysis, it has simple concepts to understand. Therefore, simplicity of the proposed method is its main advantage over previous works.

Consequently, the proposed MRAS is unique. This paper is organized as follows. In Section 2, the dynamic model of DFIG is presented. The proposed observer structure is described in Section 3. Section 4 presents stability analysis of the suggested MRAS-based speed estimation algorithm. Simulation and practical results are presented in sections 5 and 6, respectively. Finally, conclusions are included in Section 7.

2. DYNAMIC MODELLING OF DFIG

Figure 1 shows the equivalent circuit of a DFIG in the abc frame. Assuming abc fluxes as state variables, the basic equations of a DFIG can be written as follows [19]:

\[
\frac{d}{dt}\begin{bmatrix}
\psi_{\alpha s} \\
\psi_{\beta s} \\
\psi_{\alpha r} \\
\psi_{\beta r}
\end{bmatrix} = \begin{bmatrix}
\frac{-R_s}{\sigma L_s} & 0 & \frac{R_s L_m}{\sigma L_s L_r} & 0 \\
0 & \frac{-R_s}{\sigma L_s} & 0 & \frac{R_s L_m}{\sigma L_s L_r} \\
\frac{R_r L_m}{\sigma L_s L_r} & 0 & \frac{-R_r}{\sigma L_r} & -\omega_m \\
0 & \frac{R_r L_m}{\sigma L_s L_r} & \omega_m & \frac{-R_r}{\sigma L_r}
\end{bmatrix}
\begin{bmatrix}
\psi_{\alpha s} \\
\psi_{\beta s} \\
\psi_{\alpha r} \\
\psi_{\beta r}
\end{bmatrix}
\]

(1)

where \( \sigma \) is leakage coefficient equals \( 1 - \frac{L_m^2}{L_s L_r} \) and current and flux relations are as follows:

\[
\begin{bmatrix}
\psi_{\alpha s} \\
\psi_{\beta s} \\
\psi_{\alpha r} \\
\psi_{\beta r}
\end{bmatrix} = \begin{bmatrix}
L_s & 0 & L_s & 0 \\
0 & L_s & L_m & 0
\end{bmatrix}
\begin{bmatrix}
i_{\alpha s} \\
i_{\beta s} \\
i_{\alpha r} \\
i_{\beta r}
\end{bmatrix}
\]

(2)
\[
\begin{align*}
[\psi_{\alpha\alpha}] &= \begin{bmatrix} L_m & 0 \\ 0 & L_m \end{bmatrix} [i_{\alpha\alpha}] + \begin{bmatrix} L_r & 0 \\ 0 & L_r \end{bmatrix} [i_{\beta\alpha}] \\
[\psi_{\alpha\beta}] &= \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} [i_{\alpha\beta}] + \begin{bmatrix} 0 & 0 \\ 0 & 0 \end{bmatrix} [i_{\beta\beta}]
\end{align*}
\]

From Eq. (7), stator current components can be obtained as follows:
\[
\begin{align*}
[i_{\alpha\alpha}] &= \frac{\psi_{\alpha\alpha} - L_m i_{\beta\alpha}}{L_s} \\
[i_{\beta\beta}] &= \frac{\psi_{\alpha\beta} - L_m i_{\beta\beta}}{L_s}
\end{align*}
\]

Equation (10) is considered as the reference model of the MRAS based observer. By replacing Eq. (8) into Eq. (10) and after simplification, we have,
\[
P_{\text{est}} = \frac{3}{2} L_s \left[ V_{\alpha\alpha} i_{\beta\alpha} + V_{\beta\beta} i_{\beta\beta} - L_m V_{\alpha\alpha} i_{\alpha\alpha} - L_m V_{\beta\beta} i_{\beta\beta} \right]
\]

Stator flux components of Eq. (11) can be obtained as follows:
\[
\begin{align*}
[i_{\alpha\alpha}] &= \int (V_{\alpha\alpha} - R_s i_{\alpha\alpha}) dt \\
[i_{\beta\beta}] &= \int (V_{\beta\beta} - R_s i_{\beta\beta}) dt
\end{align*}
\]

3. DESCRIPTION OF OBSERVER STRUCTURE

The suggested MRAS based speed observer is introduced and described in this section. It is well-known that any MRAS based observer consists of three main blocks: reference model, adjustable model, and adaptation mechanism [20]. Fig. 2 depicts a general block diagram of the proposed algorithm. Active power is applied in the equations of reference and adjustable models. The adjustable model is extracted in a way that includes speed as a parameter.

By rewriting (2), we have,
\[
\begin{align*}
[\psi_{\alpha\alpha}] &= L_m [i_{\alpha\alpha}] + L_r [i_{\beta\alpha}] \\
[\psi_{\beta\beta}] &= L_m [i_{\alpha\beta}] + L_r [i_{\beta\beta}]
\end{align*}
\]
4. STABILITY ANALYSIS

In this section, a small signal model of the proposed MRAS observer is extracted for stability analysis. It is assumed that a small signal disturbance is given to the system in any stable operating point. It is expected that the overall system is to be stable. The adjustable model of the proposed algorithm can be rewritten as follows:

$$ P_{st} = \frac{3}{2L_s} \left[ \hat{V}_s^* - L_s \Re \left( \hat{V}_s \left( i, e^{j\gamma_m} \right)^* \right) \right] $$ (13)

If $\gamma_m$ is considered as real value, $P_{st}$ can be considered as $P_s$. Therefore,

$$ P_s = \frac{3}{2L_s} \left[ \hat{V}_s^* - L_s \Re \left( \hat{V}_s \left( i, e^{j\gamma_m} \right)^* \right) \right] $$ (14)

The established error, $\varepsilon_r$, is then as follows:

$$ \varepsilon_r = P_s - P_{st} = \Delta P $$ (15)

In Fig. 4, phasor diagram of the small signal model is illustrated.

$$ \varepsilon_r = \frac{3L_m}{2L_s} \left| V_s \right| \left| i_r \right| \sin \theta \Delta \theta $$

(17)

In the steady state conditions $\varepsilon_r$ is a function of inner product of $\hat{V}_s$ and $\hat{i}_r^*$, where $\theta$ is the angle difference between those vectors. From Fig. 4, we have,

$$ \Delta \gamma_m = \hat{\gamma}_m - \gamma_m = \theta' - \theta $$

(18)

Therefore,

$$ \varepsilon_r = \frac{3L_m}{2L_s} \left| V_s \right| \left| i_r \right| \sin \theta \Delta \gamma_m $$

(19)

Using Eq. (18) and Fig. 3, small signal block diagram for stability analysis is illustrated in Fig. 5.

Since, the speed range of the DFIG is usually set to [0.7, 1.3] p.u. [19], in order to establish the appropriate speed range of the estimator, the output of the hysteresis comparator is set to [0, 20$\omega_0$] p.u. [21, 22], where $\omega_0$ is the electrical frequency of the mains. For correct operation, the selected bandwidth for hysteresis block must be larger than the values of speed range of DFIG. Therefore, the nearest integers are chosen as hysteresis bandwidths. Also, in Fig. 5, $T_s$ is the sampling time.

Stability analysis is based on the sliding mode conditions, in which a system is stable when the product of error ($\varepsilon_r$) and error derivate ($\frac{d\varepsilon_r}{dt}$) leads to a negative result. Using Fig. 5 the following relation can be extracted:

$$ \frac{d\varepsilon_r}{dt} = \frac{3L_m}{2L_s} \left| V_s \right| \left| i_r \right| \sin \theta \omega_0 (u - \omega_m) $$

(20)

In Fig. 5, $u$ is the output signal of the hysteresis block. As it mentioned previously, according to hysteresis block output, which is 0 or 2, we have,
Finally, from Eq. (21) the stability condition can be defined as Eq. (22) in every operating point.

\[
|V_s| \neq 0, \quad \sin \theta < 0
\]  

(22)

It can be concluded from Eq. (21) and Fig. 4 that \(i_r^s\) must be lag due to \(V_s\), for stable operation of proposed observer.

5. SIMULATION RESULTS

Speed tracking of the proposed method is confirmed by simulation results, which is presented in this section. A 1.5 MW DFIG is simulated using MATLAB/Simulink software and its parameters are presented in the Appendix. Fig. 6 shows speed tracking capability of the MRAS-based observer where wind speed changes from 15 to 9 m/s. Fig. 7 illustrates speed tracking of the observer at the sub-synchronous condition where wind speed changes from 15 to 6 m/s. As can be seen, the produced error of the suggested speed estimation algorithm is less than 0.05 p.u.

Moreover, to confirm stability condition (21), the angle between \(V_s\) and \(i_r^s\) is shown in Fig. 8. It can be proved that \(\sin \theta < 0\) is valid for all simulated states.

6. PRACTICAL RESULTS

A laboratory setup is applied to prove some dynamic behaviours of the proposed algorithm. It consists of a wound rotor induction machine (WRIM) connected to the back-to-back converters. Also, a DC motor is coupled mechanically to the WRIM to play the role of a wind turbine. A digital 16-bit dsPIC30F4011 controller is used to generate adequate switching signals of the IGBTs [23]. Furthermore, PCI-1716 and PCLD-8710 I/O boards are used for real-time evaluation of the proposed method.

Fig. 6. Speed tracking capability of proposed MRAS-based observer a) wind speed b) real and estimated speed.

Fig. 7. Speed tracking capability of proposed MRAS-based observer in the sub-synchronous mode a) wind speed b) real and estimated speed.
A brushless DC (BLDC) machine is adjusted and used as a speed sensor. It is coupled to the WRIM and works as a generator. The output voltage of the BLDC is relative with its speed. The IM parameters are presented in the Appendix and Fig. 9 shows the general block diagram of the experimental setup.

Fig. 10 shows steady state operation of the IM where machine speed is fixed at 3000 rpm. The rotor current of the IM is also illustrated in the same figure. Speed tracking of the observer is depicted in Fig. 11 where speed changes from 3050 to 3500 rpm, and vice versa. The speed tracking capability of the observer in practical conditions is also acceptable.
7. CONCLUSIONS

A novel MRAS-based observer is described in this paper. Active power of DFIG is selected as state variable in the structure of the proposed observer. In the adjustable model of the observer, stator currents are transformed to the rotor frame to reveal rotor speed in its formulation. The suggested adaptation mechanism is based on a hysteresis block. The formulation of the MRAS observer in this paper, is unique. Stability of the observer is analysed on the basis of sliding-mode conditions, in detail. The enhanced stability condition is confirmed in the simulation studies. Simulation and practical results show the stable and effective operation of the suggested MRAS-based observer, particularly at the speed tracking. Simulations are performed using MATLAB/Simulink software and practical results are obtained using a DSPIC based microprocessor and a WRIM.

Appendix A.

Table 1. Parameters of the simulated DFIG

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<tr>
<th>Parameter</th>
<th>Value</th>
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<tr>
<td>Nominal Power</td>
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<td>Nominal Voltage</td>
<td>575 V</td>
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<td>Frequency</td>
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<tr>
<td>$L_{ss}$</td>
<td>0.023 pu</td>
</tr>
<tr>
<td>$R_s$</td>
<td>0.18 p.u</td>
</tr>
<tr>
<td>$L_r$</td>
<td>0.016 pu</td>
</tr>
<tr>
<td>$L_m$</td>
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</tr>
<tr>
<td>Pairs of poles</td>
<td>2.9 pu</td>
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<tr>
<td>Moment of inertia</td>
<td>0.685 Kg.m²</td>
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Table 2. Parameters of the DFIG, used for practical results

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</tr>
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<td>Nominal Voltage</td>
<td>120 V</td>
</tr>
<tr>
<td>Frequency</td>
<td>50 Hz</td>
</tr>
<tr>
<td>$L_{ss}$</td>
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<tr>
<td>$R_s$</td>
<td>1.6 Ω</td>
</tr>
<tr>
<td>$L_r$</td>
<td>0.012 H</td>
</tr>
<tr>
<td>$L_m$</td>
<td>0.379 H</td>
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<td>Pairs of poles</td>
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<tr>
<td>Moment of inertia</td>
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REFERENCES


